

Precision Measurement of Decay Dynamics in $D^{0(+)} \rightarrow \pi^{-(0)} \ell^+ \nu_\ell$

M. Ablikim¹, M. N. Achasov^{4,c}, P. Adlarson⁸³, X. C. Ai⁸⁹, C. S. Akondi^{31A,31B}, R. Aliberti³⁹, A. Amoroso^{82A,82C}, Q. An^{78,65,†}, Y. H. An⁸⁹, M. S. Anderson³⁹, Y. Bai⁶³, O. Bakina⁴⁰, H. R. Bao⁷¹, X. L. Bao⁵⁰, M. Barbaggioanni^{82C}, V. Batzskaya^{1,49}, K. Begzsuren³⁵, N. Berger³⁹, M. Berlowski⁴⁹, M. B. Bertani^{30A}, D. Bettoni^{31A}, F. Bianchi^{82A,82C}, E. Bianco^{82A,82C}, A. Bortone^{82A,82C}, I. Boyko⁴⁰, R. A. Briere⁵, A. Brueggemann⁷⁵, D. Cabiatì^{82A,82C}, H. Cai⁸⁴, M. H. Cai^{42,k,l}, X. Cai^{1,65}, A. Calcaterra^{30A}, G. F. Cao^{1,71}, N. Cao^{1,71}, S. A. Cetin^{69A}, X. Y. Chai^{51,h}, J. F. Chang^{1,65}, T. T. Chang⁴⁸, G. R. Che⁴⁸, Y. Z. Che^{1,65,71}, C. H. Chen¹⁰, Chao Chen¹, G. Chen¹, H. S. Chen^{1,71}, H. Y. Chen²⁰, M. L. Chen^{1,65,71}, S. J. Chen⁴⁷, S. M. Chen⁶⁸, T. Chen^{1,71}, W. Chen⁵⁰, X. R. Chen^{34,71}, X. T. Chen^{1,71}, X. Y. Chen^{12,g}, Y. B. Chen^{1,65}, Y. Q. Chen¹⁶, Z. K. Chen⁶⁶, J. Cheng⁵⁰, L. N. Cheng⁴⁸, S. K. Choi¹¹, X. Chu^{12,g}, G. Cibinetto^{31A}, F. Cossio^{82C}, J. Cottee-Meldrum⁷⁰, H. L. Dai^{1,65}, J. P. Dai⁸⁷, X. C. Dai⁶⁸, A. Dbeyssi¹⁹, R. E. de Boer³, D. Dedovich⁴⁰, C. Q. Deng⁸⁰, Z. Y. Deng¹, A. Denig³⁹, I. Denisenko⁴⁰, M. Destefanis^{82A,82C}, F. De Mori^{82A,82C}, E. Di Fiore^{31A,31B}, X. X. Ding^{51,h}, Y. Ding⁴⁴, Y. X. Ding³², J. Dong^{1,65}, L. Y. Dong^{1,71}, M. Y. Dong^{1,65,71}, X. Dong⁸⁴, Z. J. Dong⁶⁶, M. C. Du¹, S. X. Du⁸⁹, Shaoxu Du^{12,g}, X. L. Du^{12,g}, Y. Q. Du⁸⁴, Y. Y. Duan⁶¹, Z. H. Duan⁴⁷, P. Egorov^{40,a}, G. F. Fan⁴⁷, J. J. Fan²⁰, K. X. Fan⁶⁶, Y. H. Fan⁵⁰, J. Fang^{1,65}, Jin Fang⁶⁶, S. S. Fang^{1,71}, W. X. Fang¹, Y. Q. Fang^{1,65,†}, L. Fava^{82B,82C}, F. Feldbauer³, G. Felici^{30A}, C. Q. Feng^{78,65}, J. H. Feng¹⁶, Q. X. Feng^{42,k,l}, Y. T. Feng^{78,65}, M. Fritsch³, C. D. Fu¹, J. L. Fu⁷¹, Y. W. Fu^{1,71}, H. Gao⁷¹, Xu Gao³⁸, Y. Gao^{78,65}, Y. N. Gao^{51,h}, Y. Y. Gao³², Yunong Gao²⁰, Z. Gao⁴⁸, S. Garbolino^{82C}, I. Garzia^{31A,31B}, L. Ge⁶³, P. T. Ge²⁰, Z. W. Ge⁴⁷, C. Geng⁶⁶, A. Gilman⁷⁶, K. Goetzen¹³, J. Gollub³, J. B. Gong^{1,71}, J. D. Gong³⁸, L. Gong⁴⁴, W. X. Gong^{1,65}, W. Gradl³⁹, M. Greco^{82A,82C}, M. D. Gu⁵⁶, M. H. Gu^{1,65}, C. Y. Guan^{1,71}, A. Q. Guo³⁴, H. Guo⁵⁵, J. N. Guo^{12,g}, L. B. Guo⁴⁶, M. J. Guo⁵⁵, R. P. Guo⁵⁴, X. Guo⁵⁵, Y. P. Guo^{12,g}, Z. Guo^{78,65}, A. Guskov^{40,a}, J. Gutierrez²⁹, J. Y. Han^{78,65}, T. T. Han¹, X. Han^{78,65}, F. Hanisch³, K. D. Hao^{78,65}, X. Q. Hao²⁰, F. A. Harris⁷², C. Z. He^{51,h}, K. K. He^{17,47}, K. L. He^{1,71}, F. H. Heinsius³, C. H. Heinz³⁹, Y. K. Heng^{1,65,71}, C. Herold⁶⁷, P. C. Hong³⁸, G. Y. Hou^{1,71}, X. T. Hou^{1,71}, Y. R. Hou⁷¹, Z. L. Hou¹, H. M. Hu^{1,71}, J. F. Hu^{62,j}, Q. P. Hu^{78,65}, S. L. Hu^{12,g}, T. Hu^{1,65,71}, Y. Hu¹, Y. X. Hu⁸⁴, Z. M. Hu⁶⁶, G. S. Huang^{78,65}, K. X. Huang⁶⁶, L. Q. Huang^{34,71}, P. Huang⁴⁷, X. T. Huang⁵⁵, Y. P. Huang¹, Y. S. Huang⁶⁶, T. Hussain⁸¹, N. Hüskens³⁹, N. in der Wiesche⁷⁵, J. Jackson²⁹, Q. Ji¹, Q. P. Ji²⁰, W. Ji^{1,71}, X. B. Ji^{1,71}, X. L. Ji^{1,65}, Y. Y. Ji¹, L. K. Jia⁷¹, X. Q. Jia⁵⁵, D. Jiang^{1,71}, S. J. Jiang¹⁰, X. S. Jiang^{1,65,71}, Y. Jiang⁷¹, J. B. Jiao⁵⁵, J. K. Jiao³⁸, Z. Jiao²⁵, L. C. L. Jin¹, S. Jin⁴⁷, Y. Jin⁷³, M. Q. Jing⁵⁶, X. M. Jing⁷¹, T. Johansson⁸³, S. Kabana³⁶, X. L. Kang¹⁰, X. S. Kang⁴⁴, B. C. Ke⁸⁹, V. Khachatryan²⁹, A. Khoukaz⁷⁵, O. B. Kolcu^{69A}, B. Kopf³, L. Kröger⁷⁵, L. Krümmel³, Y. Y. Kuang⁸⁰, X. Kui^{1,71}, N. Kumar²⁸, A. Kupsc^{49,83}, W. Kühn⁴¹, Q. Lan⁸⁰, W. N. Lan²⁰, T. T. Lei^{78,65}, M. Lellmann³⁹, T. Lenz³⁹, C. Li⁵², C. H. Li⁴⁶, C. K. Li⁴⁸, Chunkai Li²¹, Cong Li⁴⁸, D. M. Li⁸⁹, F. Li^{1,65}, G. Li¹, H. B. Li^{1,71}, H. J. Li²⁰, H. L. Li⁸⁹, H. N. Li^{62,j}, H. P. Li⁴⁸, Hui Li⁴⁸, J. N. Li³², J. S. Li⁶⁶, J. W. Li⁵⁵, K. Li¹, K. L. Li^{42,k,l}, L. J. Li^{1,71}, L. K. Li²⁶, Lei Li⁵³, M. H. Li⁴⁸, M. R. Li^{1,71}, M. T. Li⁵⁵, P. L. Li⁷¹, P. R. Li^{42,k,l}, Q. M. Li^{1,71}, Q. X. Li⁵⁵, R. Li^{18,34}, S. Li⁸⁹, S. X. Li⁸⁹, S. Y. Li⁸⁹, Shanshan Li^{27,i}, T. Li⁵⁵, T. Y. Li⁴⁸, W. D. Li^{1,71}, W. G. Li^{1,†}, X. Li^{1,71}, X. H. Li^{78,65}, X. K. Li^{51,h}, X. L. Li⁵⁵, X. Y. Li^{78,65}, X. Z. Li⁶⁶, Y. Li²⁰, Y. H. Li⁴⁸, Y. B. Li⁸⁵, Y. C. Li⁶⁶, Y. G. Li⁷¹, Y. P. Li³⁸, Z. H. Li⁴², Z. J. Li⁶⁶, Z. L. Li⁸⁹, Z. X. Li⁴⁸, Z. Y. Li⁸⁷, C. Liang⁴⁷, H. Liang^{78,65}, Y. F. Liang⁶⁰, Y. T. Liang^{34,71}, Z. Z. Liang⁶⁶, G. R. Liao¹⁴, L. B. Liao⁶⁶, M. H. Liao⁶⁶, Y. P. Liao^{1,71}, J. Libby²⁸, A. Limphirat⁶⁷, C. C. Lin⁶¹, C. X. Lin³⁴, D. X. Lin^{34,71}, T. Lin¹, B. J. Liu¹, B. X. Liu⁸⁴, C. Liu³⁸, C. X. Liu¹, F. Liu¹, F. H. Liu⁵⁹, Feng Liu⁶, G. M. Liu^{62,j}, H. Liu^{42,k,l}, H. B. Liu¹⁵, H. M. Liu^{1,71}, Huihui Liu²², J. B. Liu^{78,65}, J. J. Liu²¹, K. Liu^{42,k,l}, K. Y. Liu⁴⁴, Ke Liu²³, Kun Liu⁸⁰, L. Liu⁴², L. C. Liu⁴⁸, Lu Liu⁴⁸, M. H. Liu³⁸, P. L. Liu⁵⁵, Q. Liu⁷¹, S. B. Liu^{78,65}, T. Liu¹, W. M. Liu^{78,65}, W. T. Liu⁴³, X. Liu^{42,k,l}, X. K. Liu^{42,k,l}, X. L. Liu^{12,g}, X. P. Liu^{12,g}, X. T. Liu²¹, X. Y. Liu⁸⁴, Y. Liu^{42,k,l}, Y. B. Liu⁴⁸, Yi Liu⁸⁹, Z. A. Liu^{1,65,71}, Z. D. Liu⁸⁵, Z. L. Liu⁸⁰, Z. Q. Liu⁵⁵, Z. X. Liu¹,

Z. Y. Liu⁴² , X. C. Lou^{1,65,71} , H. J. Lu²⁵ , J. G. Lu^{1,65} , X. L. Lu¹⁶ , Y. Lu⁷ , Y. H. Lu^{1,71} ,
 Y. P. Lu^{1,65} , Z. H. Lu^{1,71} , C. L. Luo⁴⁶ , J. R. Luo⁶⁶ , J. S. Luo^{1,71} , M. X. Luo⁸⁸ , T. Luo^{12,g} ,
 X. L. Luo^{1,65} , Z. Y. Lv²³ , X. R. Lyu^{71,o} , Y. F. Lyu⁴⁸ , Y. H. Lyu⁸⁹ , F. C. Ma⁴⁴ , H. L. Ma¹ ,
 Heng Ma^{27,i} , J. L. Ma^{1,71} , L. L. Ma⁵⁵ , L. R. Ma⁷³ , Q. M. Ma¹ , R. Q. Ma^{1,71} , R. Y. Ma²⁰ ,
 T. Ma^{78,65} , X. T. Ma^{1,71} , X. Y. Ma^{1,65} , F. E. Maas¹⁹ , I. MacKay⁷⁶ , M. Maggiora^{82A,82C} ,
 S. Maity³⁴ , S. Malde⁷⁶ , L. M. Mansur³⁹ , Y. J. Mao^{51,h} , Z. P. Mao¹ , S. Marcello^{82A,82C} ,
 A. Marshall⁷⁰ , F. M. Melendi^{31A,31B} , Y. H. Meng⁷¹ , Z. X. Meng⁷³ , G. Mezzadri^{31A} , H. Miao^{1,71} ,
 T. J. Min⁴⁷ , R. E. Mitchell²⁹ , X. H. Mo^{1,65,71} , A. F. Mohammad⁴⁷ , B. Moses²⁹ , N. Yu. Muchnoi^{4,c} ,
 J. Muskalla³⁹ , Y. Nefedov⁴⁰ , F. Nerling^{19,e} , H. Neuwirth⁷⁵ , Z. Ning^{1,65} , S. Nisar³³ , Q. L. Niu^{42,k,l} ,
 W. D. Niu^{12,g} , Y. Niu⁵⁵ , C. Normand⁷⁰ , S. L. Olsen^{11,71} , Q. Ouyang^{1,65,71} , I. V. Ovtin⁴ ,
 S. Pacetti^{30B,30C} , Y. Pan⁶³ , C. Y. Pang¹⁴ , A. Pathak¹¹ , Y. P. Pei^{78,65} , M. Pelizaeus³ ,
 G. L. Peng^{78,65} , H. P. Peng^{78,65} , X. J. Peng^{42,k,l} , Y. Y. Peng^{42,k,l} , K. Peters^{13,e} , K. Petridis⁷⁰ ,
 J. L. Ping⁴⁶ , R. G. Ping^{1,71} , S. Plura³⁹ , V. Prasad³⁸ , L. Pöpping³ , F. Z. Qi¹ , H. R. Qi⁶⁸ ,
 S. Qian^{1,65} , W. B. Qian⁷¹ , C. F. Qiao⁷¹ , J. H. Qiao²⁰ , J. J. Qin⁸⁰ , J. L. Qin⁶¹ , L. Q. Qin¹⁴ ,
 L. Y. Qin^{78,65} , P. B. Qin⁸⁰ , X. P. Qin⁴³ , X. S. Qin⁵⁵ , Z. H. Qin^{1,65} , J. F. Qiu¹ , Z. H. Qu⁸⁰ ,
 J. Rademacker⁷⁰ , K. Ravindran⁷⁴ , C. F. Redmer³⁹ , A. Rivetti^{82C} , M. Rolo^{82C} , G. Rong^{1,71} ,
 S. S. Rong^{1,71} , F. Rosini^{30B,30C} , Ch. Rosner¹⁹ , M. Q. Ruan^{1,65} , W. R. Ruangyoo⁶⁷ , N. Salone⁷⁹ ,
 A. Sarantsev^{40,d} , Y. Schelhaas³⁹ , M. Schernau³⁶ , K. Schoenning⁸³ , M. Scodreggio^{31A} , W. Shan²⁶ ,
 X. Y. Shan^{78,65} , Z. J. Shang^{42,k,l} , J. F. Shangguan¹⁷ , L. G. Shao^{1,71} , M. Shao^{78,65} , C. P. Shen^{12,g} ,
 H. F. Shen^{1,9} , W. H. Shen⁷¹ , X. Y. Shen^{1,71} , B. A. Shi⁷¹ , Ch. Y. Shi^{87,b} , H. Shi^{78,65} , J. L. Shi^{8,p} ,
 J. Y. Shi¹ , M. H. Shi⁸⁹ , S. Shi^{1,71} , S. Y. Shi⁸⁰ , X. Shi^{1,65} , H. L. Song^{78,65} , J. J. Song²⁰ ,
 M. H. Song⁴² , T. Z. Song⁶⁶ , W. M. Song³⁸ , Y. X. Song^{51,h,m} , Zirong Song^{27,i} , S. Sosio^{82A,82C} ,
 S. Spataro^{82A,82C} , S. Stansilaus⁷⁶ , F. Stieler³⁹ , M. Stolte³ , S. S. Su⁴⁴ , G. B. Sun⁸⁴ , G. X. Sun¹ ,
 H. Sun⁷¹ , H. K. Sun¹ , J. F. Sun²⁰ , K. Sun⁶⁸ , L. Sun⁸⁴ , R. Sun⁷⁸ , S. S. Sun^{1,71} , T. Sun^{57,f} ,
 W. Y. Sun⁵⁶ , Y. C. Sun⁸⁴ , Y. H. Sun³² , Y. J. Sun^{78,65} , Y. Z. Sun¹ , Z. Q. Sun^{1,71} , Z. T. Sun⁵⁵ ,
 H. Tabaharizato¹ , N. T. Tagsinsit⁶⁷ , C. J. Tang⁶⁰ , G. Y. Tang¹ , J. Tang⁶⁶ , J. J. Tang^{78,65} ,
 L. F. Tang⁴³ , Y. A. Tang⁸⁴ , Z. H. Tang^{1,71} , L. Y. Tao⁸⁰ , M. Tat⁷⁶ , J. X. Teng^{78,65} , J. Y. Tian^{78,65} ,
 W. H. Tian⁶⁶ , Y. Tian³⁴ , Z. F. Tian⁸⁴ , K. Yu. Todyshev⁴ , I. Uman^{69B} , E. van der Smagt³ ,
 B. Wang⁶⁶ , Bin Wang¹ , Bo Wang^{78,65} , C. Wang^{42,k,l} , Chao Wang²⁰ , Cong Wang²³ ,
 D. Y. Wang^{51,h} , F. K. Wang⁶⁶ , H. J. Wang^{42,k,l} , H. R. Wang⁸⁶ , J. Wang¹⁰ , J. H. Wang¹ ,
 J. J. Wang⁸⁴ , J. P. Wang³⁷ , K. Wang^{1,65} , L. L. Wang¹ , L. W. Wang³⁸ , M. Wang⁵⁵ , Mi Wang^{78,65} ,
 N. Y. Wang⁷¹ , P. Wang²¹ , S. Wang^{42,k,l} , Shun Wang⁶⁴ , T. Wang^{12,g} , W. Wang⁶⁶ , W. P. Wang³⁹ ,
 X. F. Wang^{42,k,l} , X. L. Wang^{12,g} , X. N. Wang^{1,71} , Xin Wang^{27,i} , Y. Wang¹ , Y. D. Wang⁵⁰ ,
 Y. F. Wang^{1,9,71} , Y. H. Wang^{42,k,l} , Y. J. Wang^{78,65} , Y. L. Wang²⁰ , Y. N. Wang⁵⁰ , Yanning Wang⁸⁴ ,
 Yaqian Wang¹⁸ , Yi Wang⁶⁸ , Yuan Wang^{18,34} , Z. Wang^{1,65} , Z. L. Wang² , Z. Q. Wang^{12,g} ,
 Z. Y. Wang^{1,71} , Zhi Wang⁴⁸ , Ziyi Wang⁷¹ , D. Wei⁴⁸ , D. H. Wei¹⁴ , D. J. Wei⁷³ , H. R. Wei⁴⁸ ,
 F. Weidner⁷⁵ , H. R. Wen³⁴ , S. P. Wen¹ , U. Wiedner³ , G. Wilkinson⁷⁶ , J. F. Wu^{1,9} , L. H. Wu¹ ,
 L. J. Wu²⁰ , Lianjie Wu²⁰ , S. G. Wu^{1,71} , S. M. Wu⁷¹ , X. W. Wu⁸⁰ , Z. Wu^{1,65} , H. L. Xia^{78,65} ,
 L. Xia^{78,65} , B. H. Xiang^{1,71} , D. Xiao^{42,k,l} , G. Y. Xiao⁴⁷ , H. Xiao⁸⁰ , Y. L. Xiao^{12,g} , Z. J. Xiao⁴⁶ ,
 C. Xie⁴⁷ , K. J. Xie^{1,71} , Y. Xie⁵⁵ , Y. G. Xie^{1,65} , Y. H. Xie⁶ , Z. P. Xie^{78,65} , T. Y. Xing^{1,71} ,
 D. B. Xiong¹ , G. F. Xu¹ , H. Y. Xu² , Q. J. Xu¹⁷ , Q. N. Xu³² , T. D. Xu⁸⁰ , X. P. Xu⁶¹ ,
 Y. Xu^{12,g} , Y. C. Xu⁸⁶ , Z. S. Xu⁷¹ , F. Yan²⁴ , L. Yan^{12,g} , W. B. Yan^{78,65} , W. C. Yan⁸⁹ ,
 W. H. Yan⁶ , W. P. Yan²⁰ , X. Q. Yan^{12,g} , Y. Y. Yan⁶⁷ , H. J. Yang^{57,f} , H. L. Yang³⁸ , H. X. Yang¹ ,
 J. H. Yang⁴⁷ , L. Y. Yang^{1,71} , R. J. Yang²⁰ , X. Y. Yang

H. Zhang^{78,65} , H. C. Zhang^{1,65,71} , H. H. Zhang⁶⁶ , H. L. Zhang⁴⁸ , H. Q. Zhang^{1,65,71} ,
H. R. Zhang^{78,65} , H. Y. Zhang^{1,65} , Han Zhang⁸⁹ , J. Zhang⁶⁶ , J. J. Zhang⁵⁸ , J. L. Zhang²¹ ,
J. Q. Zhang⁴⁶ , J. S. Zhang^{12,g} , J. W. Zhang^{1,65,71} , J. X. Zhang^{42,k,l} , J. Y. Zhang¹ , J. Z. Zhang^{1,71} ,
Jianyu Zhang⁴⁹ , Jin Zhang⁵³ , Jiyuan Zhang^{12,g} , L. M. Zhang⁶⁸ , Lei Zhang⁴⁷ , N. Zhang³⁸ ,
P. Zhang^{1,9} , Q. Zhang²⁰ , Q. Y. Zhang³⁸ , Q. Z. Zhang⁷¹ , R. Y. Zhang^{42,k,l} , S. H. Zhang^{1,71} ,
S. N. Zhang⁷⁶ , Shulei Zhang^{27,i} , X. M. Zhang¹ , X. Y. Zhang⁵⁵ , Y. T. Zhang⁸⁹ , Y. H. Zhang^{1,65} ,
Y. P. Zhang^{78,65} , Yao Zhang¹ , Yu Zhang⁸⁰ , Yu Zhang⁶⁶ , Z. Zhang³⁴ , Z. D. Zhang¹ , Z. H. Zhang¹ ,
Z. L. Zhang³⁸ , Z. X. Zhang²⁰ , Z. Y. Zhang⁸⁴ , Zh. Zh. Zhang²⁰ , Zhilong Zhang⁶¹ , Ziyang Zhang⁵⁰ ,
Ziyu Zhang⁴⁸ , G. Zhao¹ , J.-P. Zhao⁷¹ , J. Y. Zhao^{1,71} , J. Z. Zhao^{1,65} , L. Zhao¹ , Lei Zhao^{78,65} ,
M. G. Zhao⁴⁸ , R. P. Zhao⁷¹ , S. J. Zhao⁸⁹ , Y. B. Zhao^{1,65} , Y. L. Zhao⁶¹ , Y. P. Zhao⁵⁰ ,
Y. X. Zhao^{34,71} , Z. G. Zhao^{78,65} , A. Zhemchugov^{40,a} , B. Zheng⁸⁰ , B. M. Zheng³⁸ , J. P. Zheng^{1,65} ,
W. J. Zheng^{1,71} , W. Q. Zheng¹⁰ , X. R. Zheng²⁰ , Y. H. Zheng^{71,o} , B. Zhong⁴⁶ , C. Zhong²⁰ ,
X. Zhong⁴⁵ , H. Zhou^{39,55,n} , J. Q. Zhou³⁸ , S. Zhou⁶ , X. Zhou⁸⁴ , X. K. Zhou⁶ , X. R. Zhou^{78,65} ,
X. Y. Zhou⁴³ , Y. X. Zhou⁸⁶ , Y. Z. Zhou²⁰ , A. N. Zhu⁷¹ , J. Zhu⁴⁸ , K. Zhu¹ , K. J. Zhu^{1,65,71} ,
K. S. Zhu^{12,g} , L. X. Zhu⁷¹ , Lin Zhu²⁰ , S. H. Zhu⁷⁷ , T. J. Zhu^{12,g} , W. D. Zhu^{12,g} , W. J. Zhu¹ ,
W. Z. Zhu²⁰ , Y. C. Zhu^{78,65} , Z. A. Zhu^{1,71} , X. Y. Zhuang⁴⁸ , M. Zhuge⁵⁵ , J. H. Zou¹ , J. Zu³⁴ 

(BESIII Collaboration)

- ¹ *Institute of High Energy Physics, Beijing 100049, People's Republic of China*
- ² *Beihang University, Beijing 100191, People's Republic of China*
- ³ *Bochum Ruhr-University, D-44780 Bochum, Germany*
- ⁴ *Budker Institute of Nuclear Physics SB RAS (BINP), Novosibirsk 630090, Russia*
- ⁵ *Carnegie Mellon University, Pittsburgh, Pennsylvania 15213, USA*
- ⁶ *Central China Normal University, Wuhan 430079, People's Republic of China*
- ⁷ *Central South University, Changsha 410083, People's Republic of China*
- ⁸ *Chengdu University of Technology, Chengdu 610059, People's Republic of China*
- ⁹ *China Center of Advanced Science and Technology, Beijing 100190, People's Republic of China*
- ¹⁰ *China University of Geosciences, Wuhan 430074, People's Republic of China*
- ¹¹ *Chung-Ang University, Seoul, 06974, Republic of Korea*
- ¹² *Fudan University, Shanghai 200433, People's Republic of China*
- ¹³ *GSI Helmholtzcentre for Heavy Ion Research GmbH, D-64291 Darmstadt, Germany*
- ¹⁴ *Guangxi Normal University, Guilin 541004, People's Republic of China*
- ¹⁵ *Guangxi University, Nanning 530004, People's Republic of China*
- ¹⁶ *Guangxi University of Science and Technology, Liuzhou 545006, People's Republic of China*
- ¹⁷ *Hangzhou Normal University, Hangzhou 310036, People's Republic of China*
- ¹⁸ *Hebei University, Baoding 071002, People's Republic of China*
- ¹⁹ *Helmholtz Institute Mainz, Staudinger Weg 18, D-55099 Mainz, Germany*
- ²⁰ *Henan Normal University, Xinxiang 453007, People's Republic of China*
- ²¹ *Henan University, Kaifeng 475004, People's Republic of China*
- ²² *Henan University of Science and Technology, Luoyang 471003, People's Republic of China*
- ²³ *Henan University of Technology, Zhengzhou 450001, People's Republic of China*
- ²⁴ *Hengyang Normal University, Hengyang 421002, People's Republic of China*
- ²⁵ *Huangshan College, Huangshan 245000, People's Republic of China*
- ²⁶ *Hunan Normal University, Changsha 410081, People's Republic of China*
- ²⁷ *Hunan University, Changsha 410082, People's Republic of China*
- ²⁸ *Indian Institute of Technology Madras, Chennai 600036, India*
- ²⁹ *Indiana University, Bloomington, Indiana 47405, USA*
- ³⁰ *INFN Laboratori Nazionali di Frascati, (A)INFN Laboratori Nazionali di Frascati, I-00044, Frascati, Italy; (B)INFN Sezione di Perugia, I-06100, Perugia, Italy; (C)University of Perugia, I-06100, Perugia, Italy*
- ³¹ *INFN Sezione di Ferrara, (A)INFN Sezione di Ferrara, I-44122, Ferrara, Italy; (B)University of Ferrara, I-44122, Ferrara, Italy*
- ³² *Inner Mongolia University, Hohhot 010021, People's Republic of China*

- ³³ *Institute of Business Administration, University Road, Karachi, 75270 Pakistan*
- ³⁴ *Institute of Modern Physics, Lanzhou 730000, People's Republic of China*
- ³⁵ *Institute of Physics and Technology, Mongolian Academy of Sciences, Peace Avenue 54B, Ulaanbaatar 13330, Mongolia*
- ³⁶ *Instituto de Alta Investigación, Universidad de Tarapacá, Casilla 7D, Arica 1000000, Chile*
- ³⁷ *Jiangsu Ocean University, Lianyungang 222005, People's Republic of China*
- ³⁸ *Jilin University, Changchun 130012, People's Republic of China*
- ³⁹ *Johannes Gutenberg University of Mainz, Johann-Joachim-Becher-Weg 45, D-55099 Mainz, Germany*
- ⁴⁰ *Joint Institute for Nuclear Research, 141980 Dubna, Moscow region, Russia*
- ⁴¹ *Justus-Liebig-Universitaet Giessen, II. Physikalisches Institut, Heinrich-Buff-Ring 16, D-35392 Giessen, Germany*
- ⁴² *Lanzhou University, Lanzhou 730000, People's Republic of China*
- ⁴³ *Liaoning Normal University, Dalian 116029, People's Republic of China*
- ⁴⁴ *Liaoning University, Shenyang 110036, People's Republic of China*
- ⁴⁵ *Longyan University, Longyan 364000, People's Republic of China*
- ⁴⁶ *Nanjing Normal University, Nanjing 210023, People's Republic of China*
- ⁴⁷ *Nanjing University, Nanjing 210093, People's Republic of China*
- ⁴⁸ *Nankai University, Tianjin 300071, People's Republic of China*
- ⁴⁹ *National Centre for Nuclear Research, Warsaw 02-093, Poland*
- ⁵⁰ *North China Electric Power University, Beijing 102206, People's Republic of China*
- ⁵¹ *Peking University, Beijing 100871, People's Republic of China*
- ⁵² *Qufu Normal University, Qufu 273165, People's Republic of China*
- ⁵³ *Renmin University of China, Beijing 100872, People's Republic of China*
- ⁵⁴ *Shandong Normal University, Jinan 250014, People's Republic of China*
- ⁵⁵ *Shandong University, Jinan 250100, People's Republic of China*
- ⁵⁶ *Shandong University of Technology, Zibo 255000, People's Republic of China*
- ⁵⁷ *Shanghai Jiao Tong University, Shanghai 200240, People's Republic of China*
- ⁵⁸ *Shanxi Normal University, Linfen 041004, People's Republic of China*
- ⁵⁹ *Shanxi University, Taiyuan 030006, People's Republic of China*
- ⁶⁰ *Sichuan University, Chengdu 610064, People's Republic of China*
- ⁶¹ *Soochow University, Suzhou 215006, People's Republic of China*
- ⁶² *South China Normal University, Guangzhou 510006, People's Republic of China*
- ⁶³ *Southeast University, Nanjing 211100, People's Republic of China*
- ⁶⁴ *Southwest University of Science and Technology, Mianyang 621010, People's Republic of China*
- ⁶⁵ *State Key Laboratory of Particle Detection and Electronics, Beijing 100049, Hefei 230026, People's Republic of China*
- ⁶⁶ *Sun Yat-Sen University, Guangzhou 510275, People's Republic of China*
- ⁶⁷ *Suranaree University of Technology, University Avenue 111, Nakhon Ratchasima 30000, Thailand*
- ⁶⁸ *Tsinghua University, Beijing 100084, People's Republic of China*
- ⁶⁹ *Turkish Accelerator Center Particle Factory Group, (A)Istinye University, 34010, Istanbul, Turkey; (B)Near East University, Nicosia, North Cyprus, 99138, Mersin 10, Turkey*
- ⁷⁰ *University of Bristol, H H Wills Physics Laboratory, Tyndall Avenue, Bristol, BS8 1TL, UK*
- ⁷¹ *University of Chinese Academy of Sciences, Beijing 100049, People's Republic of China*
- ⁷² *University of Hawaii, Honolulu, Hawaii 96822, USA*
- ⁷³ *University of Jinan, Jinan 250022, People's Republic of China*
- ⁷⁴ *University of La Serena, Av. Raúl Bitrán 1305, La Serena, Chile*
- ⁷⁵ *University of Muenster, Wilhelm-Klemm-Strasse 9, 48149 Muenster, Germany*
- ⁷⁶ *University of Oxford, Keble Road, Oxford OX13RH, United Kingdom*
- ⁷⁷ *University of Science and Technology Liaoning, Anshan 114051, People's Republic of China*
- ⁷⁸ *University of Science and Technology of China, Hefei 230026, People's Republic of China*
- ⁷⁹ *University of Silesia in Katowice, Institute of Physics, 75 Pulku Piechoty 1, 41-500 Chorzow, Poland*
- ⁸⁰ *University of South China, Hengyang 421001, People's Republic of China*

⁸¹ *University of the Punjab, Lahore-54590, Pakistan*

⁸² *University of Turin and INFN, (A)University of Turin, I-10125, Turin, Italy; (B)University of Eastern Piedmont, I-15121, Alessandria, Italy; (C)INFN, I-10125, Turin, Italy*

⁸³ *Uppsala University, Box 516, SE-75120 Uppsala, Sweden*

⁸⁴ *Wuhan University, Wuhan 430072, People's Republic of China*

⁸⁵ *Xi'an Jiaotong University, No.28 Xianning West Road, Xi'an, Shaanxi 710049, P.R. China*

⁸⁶ *Yantai University, Yantai 264005, People's Republic of China*

⁸⁷ *Yunnan University, Kunming 650500, People's Republic of China*

⁸⁸ *Zhejiang University, Hangzhou 310027, People's Republic of China*

⁸⁹ *Zhengzhou University, Zhengzhou 450001, People's Republic of China*

[†] *Deceased*

^a *Also at the Moscow Institute of Physics and Technology, Moscow 141700, Russia*

^b *Also at the Functional Electronics Laboratory, Tomsk State University, Tomsk, 634050, Russia*

^c *Also at the Novosibirsk State University, Novosibirsk, 630090, Russia*

^d *Also at the NRC "Kurchatov Institute", PNPI, 188300, Gatchina, Russia*

^e *Also at Goethe University Frankfurt, 60323 Frankfurt am Main, Germany*

^f *Also at Key Laboratory for Particle Physics, Astrophysics and Cosmology, Ministry of Education; Shanghai Key Laboratory for Particle Physics and Cosmology; Institute of Nuclear and Particle Physics, Shanghai 200240, People's Republic of China*

^g *Also at Key Laboratory of Nuclear Physics and Ion-beam Application (MOE) and Institute of Modern Physics, Fudan University, Shanghai 200443, People's Republic of China*

^h *Also at State Key Laboratory of Nuclear Physics and Technology, Peking University, Beijing 100871, People's Republic of China*

ⁱ *Also at School of Physics and Electronics, Hunan University, Changsha 410082, China*

^j *Also at Guangdong Provincial Key Laboratory of Nuclear Science, Institute of Quantum Matter, South China Normal University, Guangzhou 510006, China*

^k *Also at MOE Frontiers Science Center for Rare Isotopes, Lanzhou University, Lanzhou 730000, People's Republic of China*

^l *Also at Lanzhou Center for Theoretical Physics, Lanzhou University, Lanzhou 730000, People's Republic of China*

^m *Also at Ecole Polytechnique Federale de Lausanne (EPFL), CH-1015 Lausanne, Switzerland*

ⁿ *Also at Helmholtz Institute Mainz, Staudinger Weg 18, D-55099 Mainz, Germany*

^o *Also at Hangzhou Institute for Advanced Study, University of Chinese Academy of Sciences, Hangzhou 310024, China*

^p *Also at Applied Nuclear Technology in Geosciences Key Laboratory of Sichuan Province, Chengdu University of Technology, Chengdu 610059, People's Republic of China*

The branching fractions of $D^0 \rightarrow \pi^- e^+ \nu_e$, $D^0 \rightarrow \pi^- \mu^+ \nu_\mu$, $D^+ \rightarrow \pi^0 e^+ \nu_e$, and $D^+ \rightarrow \pi^0 \mu^+ \nu_\mu$ are precisely measured, using 20.3 fb^{-1} of e^+e^- collision data collected at the center-of-mass energy of 3.773 GeV with the BESIII detector. The ratios of the decay widths between muon and positron channels are examined in full, across several four-momentum transfer ranges of $\ell^+ \nu_\ell$. No lepton flavor universality violation is found in the current data. From a simultaneous fit to the precisely measured partial decay rates and the first measured forward-backward asymmetries of these four decays, the product of the hadronic transition form factor, $f_+^{D \rightarrow \pi}(0)$, and the modulus of the $c \rightarrow d$ quark mixing element, $|V_{cd}|$, is measured with unprecedented precision to be $f_+^{D \rightarrow \pi}(0)|V_{cd}| = 0.1425 \pm 0.0005_{\text{stat.}} \pm 0.0003_{\text{syst.}}$. Taking the value of $|V_{cd}|$ from the standard model global fit and $f_+^{D \rightarrow \pi}(0)$ derived by the lattice quantum chromodynamics calculation as input, we obtain $f_+^{D \rightarrow \pi}(0) = 0.1425 \pm 0.0005_{\text{stat.}} \pm 0.0003_{\text{syst.}}$ and $|V_{cd}| = 0.2262 \pm 0.0008_{\text{stat.}} \pm 0.0005_{\text{syst.}} \pm 0.0018_{\text{LQCD.}}$, respectively. The precision of each result is a factor of 2-3 better than the previous best measurements. Additionally, the real and imaginary parts of the scalar current contribution in the $c \rightarrow d \ell^+ \nu_\ell$ transition are measured for the first time to be $\text{Re}(C_S^\mu) = 0.022 \pm 0.023_{\text{stat.}} \pm 0.003_{\text{syst.}}$ and $|\text{Im}(C_S^\mu)| = 0.000 \pm 0.038_{\text{stat.}} \pm 0.012_{\text{syst.}}$.

Experimental studies of semileptonic (SL) decays of heavy mesons are critical for testing the Standard Model (SM), and probing potential new physics (NP) effects

beyond the SM. In the SM, the couplings of different families of leptons to gauge bosons are expected to be equal. Recent experiments from BaBar, Belle, and

LHCb [1–5] reported anomalies in SL B decays mediated by $b \rightarrow c\ell^+\nu_\ell$ that deviate from the SM predictions up to 3σ [6, 7], indicating a hint of the violation of lepton flavor universality (LFU). Precision measurements of the branching fraction (BF) ratios and decay dynamics of SL D decays would offer important complementary information to understand these tensions.

Various NP models, including two-Higgs-doublet models [8, 9], leptoquark scenarios [10, 11], and model-independent investigations [12], suggest that the violation of LFU may arise from a scalar current (SC) contribution in weak interaction. Investigating the $c \rightarrow s(d)\ell^+\nu_\ell$ transitions in SL D decays is crucial for understanding these discrepancies [13–15]. In the $W_{\ell+\nu_\ell}$ rest frame, θ_W denotes the angle between the lepton momentum and the direction opposite to the D meson. The partial decay rates (PDRs) $\frac{d\Gamma}{dq^2}$, the forward ($\cos\theta_W > 0$) and backward ($\cos\theta_W < 0$) asymmetries $\mathcal{A}_{FB}(q^2)$ of $D \rightarrow \pi\ell^+\nu_\ell$ are dependent on a SC contribution in the $c \rightarrow d\ell^+\nu_\ell$ transition, making these studies essential for constraining the SC parameter space and potentially revealing unknown scalar bosons beyond the SM.

Accurate measurements of the decay dynamics of $D \rightarrow \pi\ell^+\nu_\ell$ also allow for precise extraction of the product $|V_{cd}|f_+^{D \rightarrow \pi}(0)$, where $|V_{cd}|$ is the Cabibbo-Kobayashi-Maskawa (CKM) matrix element and $f_+^{D \rightarrow \pi}(0)$ is the hadronic transition form factor (FF) at zero-momentum transfer. The hadronic FF can be calculated using various theoretical approaches, such as the quark model, QCD sum rules, and lattice quantum chromodynamics (LQCD) [16–27]. The precisely measured values of $f_+^{D \rightarrow \pi}(0)$ and $|V_{cd}|$ are important for testing different theoretical predictions and verifying the unitarity of the CKM matrix with higher precision.

Previously, several BF measurements and decay dynamics analyses of $D^0 \rightarrow \pi^-\ell^+\nu_\ell$ and $D^+ \rightarrow \pi^0\ell^+\nu_\ell$ were reported by BaBar [28], CLEO-c [29–32], Belle [33] and BESIII [34–36]. However, no experimental studies of the SC and the forward-backward asymmetry were reported. This Letter reports the first experimental constraints on the SC in the $D \rightarrow \pi\ell^+\nu_\ell$ decays and the precisely determined PDRs. The BFs, the hadronic FF $f_+^{D \rightarrow \pi}(0)$, and the modulus of the CKM matrix element $|V_{cd}|$, as well as tests of LFU in full and several q^2 ($= (E_{\ell^+} + E_{\nu_\ell})^2 - (\vec{p}_{\ell^+} + \vec{p}_{\nu_\ell})^2$) intervals, are reported based on analysis of 20.3 fb^{-1} [37] of e^+e^- collision data collected by the BESIII detector at the center-of-mass energy $\sqrt{s} = 3.773 \text{ GeV}$. These results supersede the previous BESIII measurements [34–36] that used a portion of the dataset presented here. Throughout this Letter, charge conjugated modes are implied unless stated otherwise.

The BESIII detector [38, 39] consists of a helium-based multilayer drift chamber (MDC), a plastic scintillator time-of-flight system (TOF), and a CsI(Tl) electromagnetic calorimeter (EMC), all enclosed in a superconduct-

ing solenoidal magnet providing a 1.0 T magnetic field. The inclusive Monte Carlo (MC) sample described in Refs. [40–46] has been validated for background simulation. The signal MC events of $D \rightarrow \pi\ell^+\nu_\ell$ are generated using the two-parameter series expansion [46], with the parameters obtained in this Letter.

The $\psi(3770)$ resonance decays mainly into a $D\bar{D}$ pair. Throughout this Letter, D refers to $D^0(D^+)$ and $\bar{D}$ refers to $\bar{D}^0(D^-)$ unless stated explicitly. If a single-tag (ST) $\bar{D}$ meson is correctly reconstructed, the presence of another D meson is guaranteed. Thus, in the system recoiling against an ST $\bar{D}$ meson, the double-tag (DT) candidates for $D^{0(+)} \rightarrow \pi^{-(0)}\ell^+\nu_\ell$ are selected. The ST $\bar{D}$ mesons are reconstructed using decay modes: $\bar{D}^0 \rightarrow K^+\pi^-, K^+\pi^-\pi^0, K^+\pi^-\pi^-\pi^+, K^+\pi^-\pi^0\pi^0$ and $K^+\pi^-\pi^-\pi^+\pi^0$; $D^- \rightarrow K^+\pi^-\pi^-, K_S^0\pi^-, K^+\pi^-\pi^-\pi^0, K_S^0\pi^-\pi^0, K_S^0\pi^+\pi^-\pi^-$ and $K^+K^-\pi^-$. The BF of the $D \rightarrow \pi\ell^+\nu_\ell$ decay is determined by

$$\mathcal{B} = \frac{N_{\text{DT}}}{N_{\text{ST}}^{\text{tot}} \bar{\epsilon}_{\text{sig}}}, \quad (1)$$

where $N_{\text{ST}}^{\text{tot}} = \sum_i N_{\text{ST}}^i$ and N_{DT} are the ST and DT yields in data, $\bar{\epsilon}_{\text{sig}} = \sum_i [(\epsilon_{\text{DT}}^i N_{\text{ST}}^i) / (\epsilon_{\text{ST}}^i N_{\text{ST}}^{\text{tot}})]$ represents the efficiency of finding the $D^{0(+)} \rightarrow \pi^{-(0)}\ell^+\nu_\ell$ decay in the presence of an ST $\bar{D}$ meson.

The selection criteria of $K^\pm, \pi^\pm, K_S^0, \pi^0$ meson candidates and photon candidates on both tag and signal sides are the same as those in Ref. [47]. The ST $\bar{D}$ mesons are selected based on two kinematic variables defined in the e^+e^- center-of-mass frame: the energy difference $\Delta E \equiv E_{\bar{D}} - E_{\text{beam}}$ and the beam-constrained mass $M_{\text{BC}} \equiv \sqrt{E_{\text{beam}}^2/c^4 - |\vec{p}_{\bar{D}}|^2/c^2}$. Here, E_{beam} is the beam energy, and $E_{\bar{D}}$ and $\vec{p}_{\bar{D}}$ are the total energy and momentum of the $\bar{D}$ candidate, respectively. If there are multiple combinations for a given ST mode, the one giving the minimum $|\Delta E|$ is retained.

For each tag mode, the ST yield and efficiency are extracted by an unbinned maximum likelihood fit to the M_{BC} distribution of the reconstructed $\bar{D}$ candidates from data and inclusive MC sample, respectively. The fit method is the same as those in Ref. [47]. The ΔE requirements, the ST yields in data, and the ST efficiencies are provided in Ref. [50]. Summing over all tag modes, the total yields of ST D^- and $\bar{D}^0$ mesons are $(19, 057.6 \pm 5.4_{\text{stat.}}) \times 10^3$ and $(10, 646.9 \pm 3.8_{\text{stat.}}) \times 10^3$, respectively.

The $D \rightarrow \pi\ell^+\nu_\ell$ candidates are reconstructed from the remaining tracks and showers that are not used in the tag side. Candidates for π^- and π^0 mesons are selected using the same criteria as those employed in the ST selection. To ensure data-MC consistency and minimize systematic uncertainties, lepton candidates are required to satisfy $|\cos\theta| < 0.80$. They are identified by using the ionization energy loss measured by the MDC, along with information from the TOF and EMC, based on which the likelihoods for positron, muon, kaon and pion hypotheses

$\mathcal{L}_{e,\mu,\pi,K}$ are calculated. Positron candidates must satisfy $\mathcal{L}_e/(\mathcal{L}_e + \mathcal{L}_\pi + \mathcal{L}_K) > 0.8$, and $\mathcal{L}_e > 0.001$. In addition, their deposited energies in the EMC are required to be greater than 0.8 times their momenta reconstructed by the MDC. The four-momenta of nearby photons are aligned with the positron momentum to partially account for energy loss due to final-state radiation (FSR). Muon candidates must satisfy $\mathcal{L}_\mu > \mathcal{L}_e$, and $\mathcal{L}_\mu > 0.001$, with energies deposited in the EMC being less than 0.3 GeV. The muons with momentum greater than 0.5 GeV/c are required to satisfy the criterion of momentum-dependent hit depth in the muon counter as used in Ref. [36]. To suppress the backgrounds from the hadronic D decays involving π^0 meson in final states, there must be no additional good charged tracks in the signal side ($N_{\text{extra}}^{\text{char}}$) and the maximum energies of extra photons ($E_{\text{extra}}^{\text{max}} \gamma$) not used in the event selection have to be less than 0.25 GeV.

To suppress the backgrounds associated with the misidentification between π^+ and ℓ^+ particles, the invariant masses of the $\pi^{-(0)}\ell^+$ combinations are required to be less than 1.80 (1.70) GeV/ c^2 for the positron (muon) channels. To further reject the peaking backgrounds from $D^0 \rightarrow K_S^0(\pi^+\pi^-)\pi^0$ and $D^+ \rightarrow \bar{K}^0\pi^+$ decays for the signal modes $D^0 \rightarrow \pi^-\mu^+\nu_\mu$ and $D^+ \rightarrow \pi^0\mu^+\nu_\mu$, we require $M_{\pi^-\mu^+}$ and $M_{D^-\mu^+}^{\text{rec}}$ ($D^-\mu^+$ recoil mass) to be outside the ranges (0.455, 0.497) GeV/ c^2 and (0.437, 0.580) GeV/ c^2 , respectively. These ranges correspond to the regions within $\pm 3\sigma$ around each fitted peak.

The undetected neutrino is inferred from the kinematic variable $M_{\text{miss}}^2 \equiv E_{\text{miss}}^2/c^2 - |\vec{p}_{\text{miss}}|^2/c^2$, which peaks around zero for signal events. The E_{miss} and $\vec{p}_{\text{miss}}$, given by $E_{\text{miss}} \equiv E_{\text{beam}} - E_\pi - E_{\ell^+}$ and $\vec{p}_{\text{miss}} \equiv \vec{p}_D - \vec{p}_\pi - \vec{p}_{\ell^+}$, are the missing energy and momentum of the DT event in the e^+e^- center-of-mass frame, respectively. Here, $E_{\pi(\ell^+)}$ and $\vec{p}_{\pi(\ell^+)}$ are the measured energy and momentum of the $\pi(\ell^+)$ candidates, respectively, and $\vec{p}_D \equiv -\hat{p}_D \sqrt{E_{\text{beam}}^2/c^2 - m_D^2 c^2}$, where $\hat{p}_D$ is the unit vector in the momentum direction of the ST $\bar{D}$ meson and m_D is the nominal $\bar{D}$ mass [49].

After imposing all selection criteria, the M_{miss}^2 distributions are shown in Fig. 1. Fits to these distributions are performed to extract the signal yields. The signal and background shapes are derived from MC simulation, with their yields floated. The signal shape is convolved with a Gaussian function with free parameters to account for resolution difference between data and MC simulation. The peaking background $D^0 \rightarrow \pi^-\pi^+\pi^0$ for the channel $D^0 \rightarrow \pi^-\mu^+\nu_\mu$ is described by its simulated shape convolved with a different Gaussian function.

The BF of each signal decay is determined using the signal yields in data (N_{DT}), the weighted signal efficiencies ($\bar{\epsilon}_{\text{sig}}$) corrected by the data-MC discrepancies, and ST $\bar{D}$ yields in data ($N_{\text{ST}}^{\text{tot}}$). The results are summarized in Table 1.

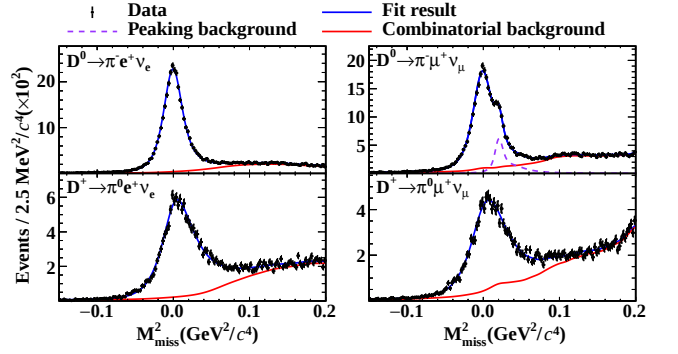


Fig. 1. Fits to the M_{miss}^2 distributions for different signal decays.

Table 1. Signal yields in data (N_{DT}), averaged signal efficiencies ($\bar{\epsilon}_{\text{sig}}$), and obtained BF for each signal decay ($\mathcal{B}_{\text{sig}}$), where the first uncertainties are statistical and the second systematic.

Decay	$\bar{\epsilon}_{\text{sig}}$ (%)	N_{DT}	$\mathcal{B}_{\text{sig}} (\times 10^{-3})$
$D^0 \rightarrow \pi^- e^+ \nu_e$	61.97	34834 ± 202	$2.950 \pm 0.017 \pm 0.017$
$D^0 \rightarrow \pi^- \mu^+ \nu_\mu$	46.84	25140 ± 330	$2.817 \pm 0.037 \pm 0.019$
$D^+ \rightarrow \pi^0 e^+ \nu_e$	39.76	15330 ± 145	$3.622 \pm 0.034 \pm 0.018$
$D^+ \rightarrow \pi^0 \mu^+ \nu_\mu$	29.52	10890 ± 135	$3.507 \pm 0.043 \pm 0.026$

The systematic uncertainties in BF measurements are discussed below. The uncertainties of ST $\bar{D}^0$ and D^- yields in data, $N_{\text{ST}}^{\text{tot}}$, are both assigned as 0.30% by varying the signal and background shapes in the M_{BC} fits. The uncertainties for tracking and particle identification (PID) of e^+ (0.20%), μ^+ (0.20%), π^- (0.20%), and π^0 reconstruction (0.17% for e^+ channels, 0.19% for μ^+ channels) are investigated using control samples of $e^+e^- \rightarrow \gamma e^+e^-$, $e^+e^- \rightarrow \gamma \mu^+\mu^-$, and hadronic DT $D\bar{D}$ events, respectively. The systematic uncertainties from $E_{\text{extra}}^{\text{max}} \gamma$ and $N_{\text{char}}^{\text{extra}}$ requirements (0.10%) are investigated using the control sample of hadronic DT $D\bar{D}$ events. The uncertainties of signal MC model (0.03%~0.13%) are estimated by comparing DT efficiencies obtained by varying the input parameters by $\pm 1\sigma$. The uncertainty of the K_S^0 veto (0.06% and 0.02%) is estimated by changing the fitted resolution based on MC simulation. The systematic uncertainty for the M_{miss}^2 fit is estimated to be (0.06%~0.54%) by varying the relative fractions of the backgrounds from $e^+e^- \rightarrow q\bar{q}$ and the dominant D background channels. The uncertainties of limited MC statistics (0.02%~0.03%), FSR effect of the positron channels (0.26% and 0.10%), and the BF of $\pi^0 \rightarrow \gamma\gamma$ (0.03%) are also included. The difference in measured BFs between the simultaneous and nominal fit methods (using single yield-weighted efficiencies) is taken as a systematic uncertainty (0.10% and 0.10%). Adding all systematic uncertainties in quadrature gives the total systematic uncertainty for each signal decay. They are 0.58%, 0.66%, 0.50%, and 0.73% for the $D^0 \rightarrow \pi^- e^+ \nu_e$, $D^0 \rightarrow \pi^- \mu^+ \nu_\mu$,

$D^+ \rightarrow \pi^0 e^+ \nu_e$, and $D^+ \rightarrow \pi^0 \mu^+ \nu_\mu$ channels, respectively.

With the measured BFs, we determine the BF ratios between muon and positron channels to be $\mathcal{R}_{\text{LFU}}^0 = 0.947 \pm 0.014_{\text{stat.}} \pm 0.005_{\text{syst.}}$ and $\mathcal{R}_{\text{LFU}}^+ = 0.973 \pm 0.015_{\text{stat.}} \pm 0.006_{\text{syst.}}$ for the D^0 and D^+ meson decay separately. Here, the systematic uncertainties in ST yields, π^-/ℓ^+ tracking and PID, and π^0 reconstruction cancel. The results are consistent with the SM prediction of 0.985 ± 0.002 [48] within 2.5σ and 0.8σ , respectively. When combining the D meson lifetimes $\tau_{D^0} = (410.3 \pm 1.0)$ fs and $\tau_{D^+} = (1033 \pm 5)$ fs [49], we determine the BF ratios between D^0 and D^+ channels, ($\mathcal{R}_{\text{IS}}^\ell \equiv \frac{\Gamma(D^0 \rightarrow \pi \ell^+ \nu_\ell)}{2\Gamma(D^+ \rightarrow \pi \ell^+ \nu_\ell)}$), to be $\mathcal{R}_{\text{IS}}^e = 1.025 \pm 0.013_{\text{stat.}} \pm 0.007_{\text{syst.}}$ and $\mathcal{R}_{\text{IS}}^\mu = 1.011 \pm 0.019_{\text{stat.}} \pm 0.010_{\text{syst.}}$. The systematic uncertainties cancel similarly to the $\mathcal{R}_{\text{LFU}}$ calculation, while those from the lifetimes are added. These ratios support isospin conservation in these decays.

To study the decay dynamics of $D \rightarrow \pi \ell^+ \nu_\ell$, candidate events are divided into different q^2 intervals with a step size of $0.3 \text{ GeV}^2/c^4$. The q^2 -binned PDRs $\Delta\Gamma_i^{\text{msr}}$ are determined as $\Delta\Gamma_i^{\text{msr}} = \frac{N_{\text{pro}}^i}{\tau_D \cdot N_{\text{ST}}^{\text{tot}}}$, where τ_D is the D meson lifetime [49] and $N_{\text{pro}}^i = \sum_j^{N_{\text{bins}}} (\varepsilon^{-1})_{ij} N_{\text{DT}}^j$ is the corresponding produced signal SL yield. Here, the observed SL yield (N_{DT}^j) is obtained by fitting the corresponding M_{miss}^2 distribution in the j -th reconstructed q^2 interval. The ε^{-1} is the inverse matrix of the signal efficiency matrix ε , which includes the migrations between the generated and reconstructed q^2 intervals choice. In addition to the systematic uncertainties in the BF measurement, two additional uncertainties arise from τ_D [49] and the different q^2 interval choice. Detailed information of correlated and uncorrelated systematic uncertainties are given in Ref. [50].

The q^2 -binned forward-backward asymmetry in the i th q^2 interval is defined as

$$\mathcal{A}_{FB,i} = \int_{q_{\text{min}}^2(i)}^{q_{\text{max}}^2(i)} \mathcal{A}_{FB}(q^2) \frac{d\Gamma}{dq^2} dq^2 \bigg/ \int_{q_{\text{min}}^2(i)}^{q_{\text{max}}^2(i)} \frac{d\Gamma}{dq^2} dq^2. \quad (2)$$

They are measured with

$$\mathcal{A}_{FB,i}^{\text{msr}} = \frac{N_{\text{pro}}(\cos \theta_W > 0, q_i^2) - N_{\text{pro}}(\cos \theta_W < 0, q_i^2)}{N_{\text{pro}}(\cos \theta_W > 0, q_i^2) + N_{\text{pro}}(\cos \theta_W < 0, q_i^2)}, \quad (3)$$

similarly to the PDRs. Except those from π^- tracking and PID (π^0 reconstruction), ℓ^+ tracking and PID, M_{miss}^2 fit, and MC statistics, other systematic uncertainties of N_{pro} cancel in the calculation of $\mathcal{A}_{FB,i}$. They are estimated similarly to the PDRs.

The measured PDRs of $D \rightarrow \pi \ell^+ \nu_\ell$ and the calculated $\mathcal{R}_{\text{LFU}}$ in each q^2 interval are shown in Figs. 2(a-h, m, n). The determined $\mathcal{A}_{FB}(q^2)$ for $D \rightarrow \pi \ell^+ \nu_\ell$ are shown in Figs. 2 (i-l).

The theoretical decay rates $\Delta\Gamma_i^{\text{th}} = \int_{q_{\text{min}}^2(i)}^{q_{\text{max}}^2(i)} \frac{d\Gamma}{dq^2} dq^2$

and forward-backward asymmetries $\mathcal{A}_{FB}^{\text{th}}(q^2)$ are expressed as [20]

$$\frac{d\Gamma}{dq^2} = X \mathcal{N}(q^2) \left(1 - \frac{m_\ell^2}{q^2}\right)^2 \left[\left(1 + \frac{m_\ell^2}{2q^2}\right) |\mathcal{H}_0(q^2)|^2 + \frac{3m_\ell^2}{2q^2} |\mathcal{H}_t(q^2)|^2 \right], \quad (4)$$

and

$$\mathcal{A}_{FB}^{\text{th}}(q^2) = \frac{3\mathcal{N}(q^2)}{2} \frac{1}{d\Gamma/dq^2} \left(1 - \frac{m_\ell^2}{q^2}\right)^2 \frac{m_\ell^2}{q^2} \text{Re}(\mathcal{H}_0(q^2)\mathcal{H}_t(q^2)). \quad (5)$$

The term $\mathcal{N}(q^2) = \frac{G_F^2 |V_{cd}|^2 |\mathbf{q}| q^2}{96\pi^3 m_D^2}$ is the overall normalization factor, incorporating the Fermi coupling constant G_F , the CKM matrix element $|V_{cd}|$, and the D meson mass m_D [49]. Here, $\mathbf{q}$ denotes the four-momentum of the $\ell^+ \nu_\ell$ system in the D meson rest frame, and m_ℓ^+ is the lepton mass. In Eq. 4, X is a multiplicative isospin factor, which is 1 for $D^0 \rightarrow \pi^- \ell^+ \nu_\ell$ and $1/2$ for $D^+ \rightarrow \pi^0 \ell^+ \nu_\ell$.

The hadronic helicity amplitudes $\mathcal{H}_{0(t)}(q^2)$ are expressed as

$$\mathcal{H}_0(q^2) = \frac{2m_D |\mathbf{q}|}{\sqrt{q^2}} f_+^{D \rightarrow \pi}(q^2), \mathcal{H}_t(q^2) = \frac{m_D^2 - m_\pi^2}{\sqrt{q^2}} f_0^\pi(q^2), \quad (6)$$

and with SC contributions, $\mathcal{H}_t(q^2)$ is modified as

$$\mathcal{H}_t(q^2) = \left(1 + C_S^\ell \frac{q^2}{m_\ell(m_d - m_c)}\right) \frac{m_D^2 - m_\pi^2}{\sqrt{q^2}} f_0^{D \rightarrow \pi}(q^2). \quad (7)$$

Here, $f_+^{D \rightarrow \pi}(q^2)$ and $f_0^{D \rightarrow \pi}(q^2)$ are the vector and scalar FFs, respectively. The $C_S^\ell = C_R^\ell + C_L^\ell$ represents the scalar combination of Wilson coefficients for the right and left-handed SCs [13–15]. The values $m_c = 1.273 \text{ GeV}/c^2$ and $m_d = 4.67 \text{ MeV}/c^2$ [49] are the $\overline{\text{MS}}$ masses at the energy scale $\mu = m_s$ and 2 GeV , respectively; m_π is the pion mass. The Wilson coefficient C_S^ℓ can be complex in both positron and muon channels. For the muon channels, angular observables allow $\text{Re}(C_S^\mu)$ and $\text{Im}(C_S^\mu)$ to be treated separately. For the positron channels, the PDRs are only sensitive to $|C_S^e|$, and forward-backward asymmetry is not affected by the scalar contribution; thus only $|C_S^e|$ is considered.

The hadronic FFs $f_+^{D \rightarrow \pi}(q^2)$ are parameterized using a two-parameter series expansion [51], which is a function of the product $f_+^{D \rightarrow \pi}(0)|V_{cd}|$ and the shape parameter r_1 . For $f_0^{D \rightarrow \pi}(0)$, a one-parameter expansion is used due to its much smaller contribution.

We perform a simultaneous fit to the differential decay rates and the forward-backward asymmetries of $D \rightarrow \pi \ell^+ \nu_\ell$ by minimizing

$$\chi^2 = \chi_{\Delta\Gamma}^2 + \sum \chi_{\mathcal{A}_{FB}}^2. \quad (8)$$

Here, the $\chi_{\Delta\Gamma}^2$ sums over all four signal decays while accounting for correlations between different q^2 intervals and signal decays using the total covariance matrix. For the $\sum \chi_{\mathcal{A}_{FB}}^2$, correlations between different signal decays are ignored since the only correlated uncertainty arises

from correction factors of ℓ^+ , which is limited. The χ_Ω^2 is expressed as

$$\chi_\Omega^2 = \sum_{i,j} \left(\Omega_i^{\text{msr}} - \Omega_i^{\text{th}} \right) \times C_{\Omega,ij}^{-1} \left(\Omega_j^{\text{msr}} - \Omega_j^{\text{th}} \right), \quad (9)$$

where Ω denotes $\Delta\Gamma$ or $\mathcal{A}_{\text{FB}}$ and C_{ij} is the sum of the statistical and systematic covariance matrices. Two separate fits are conducted under the hypotheses with and without a SC contribution. The results of the fit to the PDRs and the projections on $f_+^{D \rightarrow \pi}(q^2)$ are shown in the Figs. 2(a-h); and the obtained fit results are summarized in Table 2. Since LFU may not apply to the SC, depending on lepton mass, its muon coupling could exceed its positron coupling. Through a fit where C_S^μ is allowed to vary and $|C_S^e|$ is fixed to zero, the significance of non-zero C_S^μ is evaluated to be 1.6 σ relative to the null hypothesis (without SC).

Table 2. Parameters obtained from the fit with and without the SC, where the first uncertainties are statistical and the second systematic. The ndf denotes the number of degrees of freedom.

Variable	With SC	Without SC
$f_+^{D \rightarrow \pi}(0) V_{cd} $	0.1430(06)(04)	0.1425(05)(03)
r_1	-1.97(03)(01)	-1.99(03)(01)
$ C_S^e $	0.059(13)(09)	...
$\text{Re}(C_S^\mu)$	0.022(23)(03)	...
$\text{Im}(C_S^\mu)$	0.00(38)(12)	...
χ^2/ndf	75.5/75	81.0/78

In summary, this Letter reports the precise BF measurements and decay dynamics analyses of $D \rightarrow \pi \ell^+ \nu_\ell$ decays. Based on the precisely measured full and PDRs, we examine $\mathcal{R}_{\text{LFU}}^{0(+)}$ in full and separate q^2 intervals, and no evidence of LFU violation is found within the current data. By analyzing the $D \rightarrow \pi \ell^+ \nu_\ell$ decay dynamics without a SC, we obtain $f_+^{D \rightarrow \pi}(0)|V_{cd}|$. Taking the $|V_{cd}|$ given by the PDG [49] as input, we obtain the hadronic FF $f_+^{D \rightarrow \pi}(0) = 0.6339 \pm 0.0024_{\text{stat.}} \pm 0.0014_{\text{syst.}}$. The comparison of the $f_+^{D \rightarrow \pi}(0)$ obtained in this work with the previous measurements and theoretical calculations is shown in Fig. 3. Conversely, using the $f_+^{D \rightarrow \pi}(0)$ calculated in the LQCD [27], we obtain the CKM matrix element $|V_{cd}| = 0.2262 \pm 0.0008_{\text{stat.}} \pm 0.0005_{\text{syst.}} \pm 0.0018_{\text{LQCD.}}$. These results improve upon the previous best measurements [34, 52] by a factor of 2-3 in precision. In addition, the q^2 -binned angular observable forward-backward asymmetries $\mathcal{A}_{\text{FB}}$ and the constraints on the complex Wilson coefficients ($\text{Re}(C_S^\mu)$ and $\text{Im}(C_S^\mu)$) in $D \rightarrow \pi \ell^+ \nu_\ell$ are presented for the first time, which benefit searches for new scalar bosons beyond the SM.

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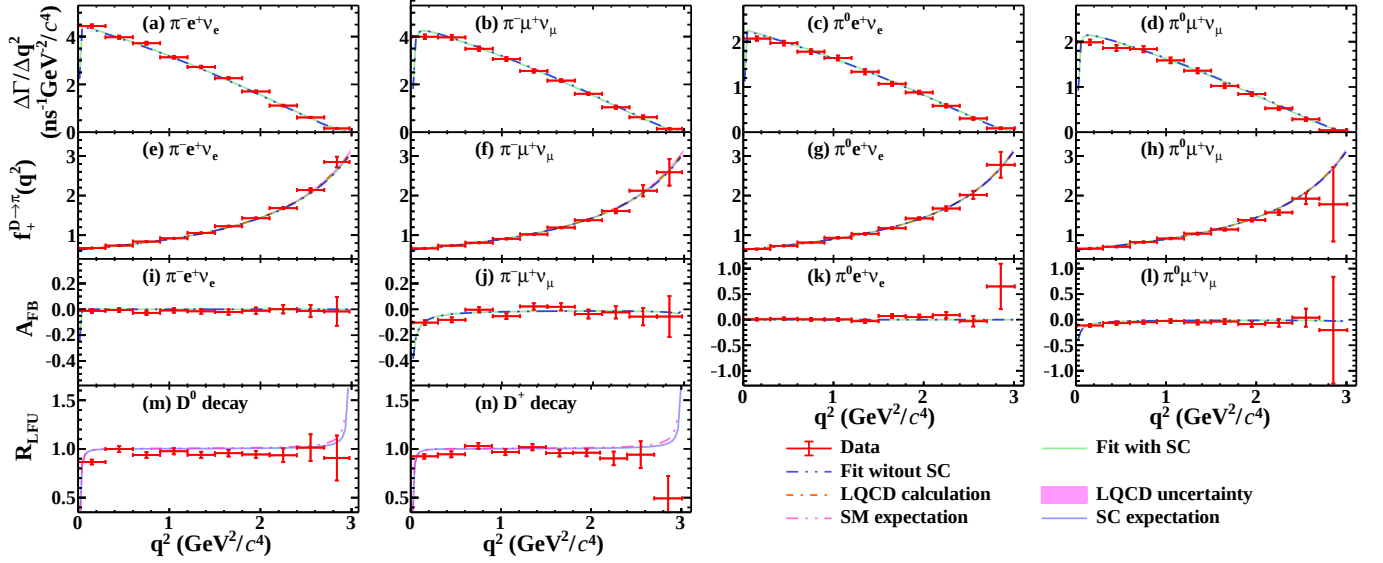


Fig. 2. Simultaneous fit to the measured $\frac{d\Gamma}{dq^2}$ (a,b,c,d) and $A_{FB}(q^2)$ (i,j,k,l), the projections on $f_+^{D \rightarrow \pi}(q^2)$ (e,f,g,h), the measured and theoretical expectation R_{LFU} (m,n).

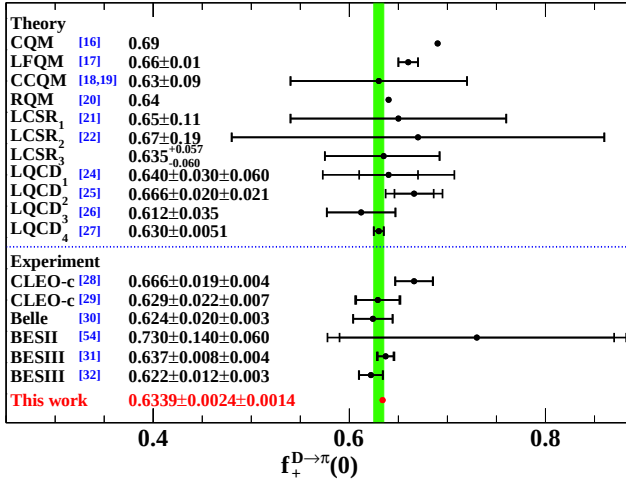


Fig. 3. Comparison of the $f_+^{D \rightarrow \pi}(0)$ measured by this work with the theoretical calculations and other experiments. The green band corresponds to the $\pm 1\sigma$ limit of the LQCD₄ calculation [27].

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